

# Cambridge International AS & A Level

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**MATHEMATICS****9709/52**

Paper 5 Probability &amp; Statistics 1

**October/November 2024****MARK SCHEME**Maximum Mark: 50

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**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2024 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

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This document consists of **18** printed pages.

**PUBLISHED****Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

**GENERIC MARKING PRINCIPLE 1:**

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

**GENERIC MARKING PRINCIPLE 2:**

Marks awarded are always **whole marks** (not half marks, or other fractions).

**GENERIC MARKING PRINCIPLE 3:**

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

**GENERIC MARKING PRINCIPLE 4:**

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

**GENERIC MARKING PRINCIPLE 5:**

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

**GENERIC MARKING PRINCIPLE 6:**

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

**Mathematics-Specific Marking Principles**

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

**PUBLISHED****Mark Scheme Notes**

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

**Types of mark**

- M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B** Mark for a correct result or statement independent of method marks.
- DM or DB** When a part of a question has two or more ‘method’ steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
  - For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
  - The total number of marks available for each question is shown at the bottom of the Marks column.
  - Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
  - Square brackets [ ] around text or numbers show extra information not needed for the mark to be awarded.

**Abbreviations**

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no ‘follow through’ from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

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Question	Answer	Marks	Guidance
1(a)	$[P(X N) =] \frac{12}{40}$	<b>B1</b>	0.3, $\frac{3}{10}$ , 30% OE.
		<b>1</b>	
1(b)	$[P(N X) =] \frac{12}{50}$	<b>B1</b>	0.24, $\frac{6}{25}$ OE.
		<b>1</b>	
1(c)	$P(N \cap X) = \frac{12}{120}, P(N) = \frac{40}{120}, P(X) = \frac{50}{120}$  $\frac{40}{120} \times \frac{50}{120} = \frac{5}{36}, 0.138[8\dots] \neq \frac{12}{120}, 0.1$ Not independent	<b>B1</b>	$P(N), P(X)$ and $P(N \cap X)$ or $P(N \text{ and } X)$ notation seen and equated to the values for $P(N), P(X)$ and $P(N \cap X)$ or $P(N \text{ and } X)$ . Calculation stated and evaluated. Not independent clearly stated. $\frac{5}{36} \neq \frac{12}{120}$ does not need to be stated. All values OE. Condone consistent use of $A, B$ etc. If values for $P(N), P(X)$ stated, accept $P(N) \times P(X) = \frac{5}{36}$ .
		<b>1</b>	

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Question	Answer	Marks	Guidance
1(d)	<b>Method 1</b>		
	$[P(0, 1, 2) =] (0.85)^8 + {}^8C_1(0.85)^7(0.15) + {}^8C_2(0.85)^6(0.15)^2$ [= 0.27249 + 0.38469 + 0.23760]	<b>M1</b>	One term of form ${}^8C_x (p)^x (1-p)^{8-x}$ . With $0 < p < 1$ , $x \neq 0$ or 8.
		<b>A1</b>	Correct unsimplified expression, no terms omitted leading to final answer.
	= 0.895	<b>B1</b>	$0.8945 \leq p \leq 0.895$ .
	<b>Method 2</b>		
	$[P(0, 1, 2) =] 1 - \{ {}^8C_3(0.85)^5(0.15)^3 + {}^8C_4(0.85)^4(0.15)^4 + {}^8C_5(0.85)^3(0.15)^5 + {}^8C_6(0.85)^2(0.15)^6 + {}^8C_7(0.85)(0.15)^7 + (0.15)^8 \}$	<b>M1</b>	One term of form ${}^8C_x (p)^x (1-p)^{8-x}$ With $0 < p < 1, x \neq 0$ or 8.
		<b>A1</b>	Correct unsimplified expression. Condone omission of final bracket '}'. If other brackets omitted, allow recovery if $1 - 0.1052[\dots]$ seen.
	= 0.895	<b>B1</b>	$0.8945 \leq p \leq 0.895$ .
		<b>3</b>	

Question	Answer	Marks	Guidance
2(a)	$\left[ \frac{9!}{2!} = \right] 181440$	<b>B1</b>	Exact value must be seen. CAO.
		<b>1</b>	

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Question	Answer	Marks	Guidance												
2(b)	<b>Method 1</b>														
	<table><tr><td>Scenario number of letters between As</td><td></td><td></td></tr><tr><td>A A [ ^ ^ ^ ^ ^ ^ ]</td><td><math>7! \times 8</math> or <math>8!</math></td><td>[ = 40320]</td></tr><tr><td>A ^ A [ ^ ^ ^ ^ ^ ^ ]</td><td><math>7! \times 7</math></td><td>[ = 35280]</td></tr><tr><td>A ^ ^ A [ ^ ^ ^ ^ ^ ^ ]</td><td><math>7! \times 6</math></td><td>[ = 30240]</td></tr></table>	Scenario number of letters between As			A A [ ^ ^ ^ ^ ^ ^ ]	$7! \times 8$ or $8!$	[ = 40320]	A ^ A [ ^ ^ ^ ^ ^ ^ ]	$7! \times 7$	[ = 35280]	A ^ ^ A [ ^ ^ ^ ^ ^ ^ ]	$7! \times 6$	[ = 30240]	<b>B1</b>	Correct outcome/value for 1 identified scenario, accept unsimplified.
	Scenario number of letters between As														
	A A [ ^ ^ ^ ^ ^ ^ ]	$7! \times 8$ or $8!$	[ = 40320]												
	A ^ A [ ^ ^ ^ ^ ^ ^ ]	$7! \times 7$	[ = 35280]												
	A ^ ^ A [ ^ ^ ^ ^ ^ ^ ]	$7! \times 6$	[ = 30240]												
		<b>M1</b>	Add values of 3 correct scenarios, no incorrect/repeated scenarios.												
	Total: $7! \times (8 + 7 + 6)$														
= 105 840	<b>A1</b>	If M1 not awarded, <b>SC B1</b> for 105840 WWW.													
<b>Method 2</b>															
<table><tr><td>Scenario number of letters between As</td><td></td><td></td></tr><tr><td>A A [ ^ ^ ^ ^ ^ ^ ]</td><td><math>8!</math></td><td>[ = 40320]</td></tr><tr><td>A ^ A [ ^ ^ ^ ^ ^ ^ ]</td><td><math>{}^7P_1 \times 7!</math> <b>or</b> <math>{}^7C_1 \times 7!</math></td><td>[ = 35280]</td></tr><tr><td>A ^ ^ A [ ^ ^ ^ ^ ^ ^ ]</td><td><math>{}^7P_2 \times 6!</math> <b>or</b> <math>{}^7C_2 \times 2 \times 6!</math></td><td>[ = 30240]</td></tr></table>	Scenario number of letters between As			A A [ ^ ^ ^ ^ ^ ^ ]	$8!$	[ = 40320]	A ^ A [ ^ ^ ^ ^ ^ ^ ]	${}^7P_1 \times 7!$ <b>or</b> ${}^7C_1 \times 7!$	[ = 35280]	A ^ ^ A [ ^ ^ ^ ^ ^ ^ ]	${}^7P_2 \times 6!$ <b>or</b> ${}^7C_2 \times 2 \times 6!$	[ = 30240]	<b>B1</b>	Correct outcome/value for 1 identified scenario, accept unsimplified.	
Scenario number of letters between As															
A A [ ^ ^ ^ ^ ^ ^ ]	$8!$	[ = 40320]													
A ^ A [ ^ ^ ^ ^ ^ ^ ]	${}^7P_1 \times 7!$ <b>or</b> ${}^7C_1 \times 7!$	[ = 35280]													
A ^ ^ A [ ^ ^ ^ ^ ^ ^ ]	${}^7P_2 \times 6!$ <b>or</b> ${}^7C_2 \times 2 \times 6!$	[ = 30240]													
	<b>M1</b>	Add values of 3 correct scenarios, no incorrect/repeated scenarios.													
Total: $8! + {}^7P_1 \times 7! + {}^7P_2 \times 6!$ <b>or</b> $8! + {}^7C_1 \times 7! + {}^7C_2 \times 2 \times 6!$															
=105 840	<b>A1</b>	If M1 not awarded, <b>SC B1</b> for 105840 WWW.													



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Question	Answer	Marks	Guidance																		
2(b)	<b>Method 3</b>																				
	<table><tr><td>Scenario number of letters between As</td><td></td><td></td></tr><tr><td>A ^ ^ ^ A [ ^ ^ ^ ^ ]</td><td>7! × 5</td><td>[ = 25200]</td></tr><tr><td>A ^ ^ ^ ^ A [ ^ ^ ^ ]</td><td>7! × 4</td><td>[ = 20160]</td></tr><tr><td>A ^ ^ ^ ^ ^ A [ ^ ^ ]</td><td>7! × 3</td><td>[ = 15120]</td></tr><tr><td>A ^ ^ ^ ^ ^ ^ A [ ^ ]</td><td>7! × 2</td><td>[ = 10080]</td></tr><tr><td>A ^ ^ ^ ^ ^ ^ ^ A</td><td>7! [× 1]</td><td>[ = 5040]</td></tr></table>	Scenario number of letters between As			A ^ ^ ^ A [ ^ ^ ^ ^ ]	7! × 5	[ = 25200]	A ^ ^ ^ ^ A [ ^ ^ ^ ]	7! × 4	[ = 20160]	A ^ ^ ^ ^ ^ A [ ^ ^ ]	7! × 3	[ = 15120]	A ^ ^ ^ ^ ^ ^ A [ ^ ]	7! × 2	[ = 10080]	A ^ ^ ^ ^ ^ ^ ^ A	7! [× 1]	[ = 5040]	<b>B1</b>	Correct outcome/value for 1 identified scenario, accept unsimplified.
	Scenario number of letters between As																				
	A ^ ^ ^ A [ ^ ^ ^ ^ ]	7! × 5	[ = 25200]																		
	A ^ ^ ^ ^ A [ ^ ^ ^ ]	7! × 4	[ = 20160]																		
	A ^ ^ ^ ^ ^ A [ ^ ^ ]	7! × 3	[ = 15120]																		
	A ^ ^ ^ ^ ^ ^ A [ ^ ]	7! × 2	[ = 10080]																		
	A ^ ^ ^ ^ ^ ^ ^ A	7! [× 1]	[ = 5040]																		
		<b>M1</b>	<i>their 2(a)</i> , or correct, subtract values of 5 correct scenarios, no incorrect/repeated scenarios.																		
Total = $\frac{9!}{2!} - 7! \times (5 + 4 + 3 + 2 + 1)$																					
=105 840	<b>A1</b>	If M1 not awarded, <b>SC B1</b> for 105840 WWW.																			
	<b>3</b>																				

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Question	Answer								Marks	Guidance																
3(a)	<table><tr><td><math>x</math></td><td>0</td><td>2</td><td>4</td><td>6</td><td>8</td><td>10</td><td>12</td></tr><tr><td><math>P(X = x)</math></td><td><math>\frac{3}{12}</math>, <math>\frac{1}{4}</math> 0.25</td><td><math>\frac{2}{12}</math>, <math>\frac{1}{6}</math> 0.167</td><td><math>\frac{2}{12}</math></td><td><math>\frac{2}{12}</math></td><td><math>\frac{1}{12}</math> 0.0833</td><td><math>\frac{1}{12}</math></td><td><math>\frac{1}{12}</math></td></tr></table>								$x$	0	2	4	6	8	10	12	$P(X = x)$	$\frac{3}{12}$ , $\frac{1}{4}$ 0.25	$\frac{2}{12}$ , $\frac{1}{6}$ 0.167	$\frac{2}{12}$	$\frac{2}{12}$	$\frac{1}{12}$ 0.0833	$\frac{1}{12}$	$\frac{1}{12}$	<b>B1</b>	Table with correct $x$ values and at least 2 correct probabilities. Condone any additional $x$ values if probability stated as 0.
	$x$	0	2	4	6	8	10	12																		
	$P(X = x)$	$\frac{3}{12}$ , $\frac{1}{4}$ 0.25	$\frac{2}{12}$ , $\frac{1}{6}$ 0.167	$\frac{2}{12}$	$\frac{2}{12}$	$\frac{1}{12}$ 0.0833	$\frac{1}{12}$	$\frac{1}{12}$																		
									<b>B1</b>	Four more probabilities correctly linked to the correct $x$ value, need not be in table, accept unsimplified.																
									<b>B1</b>	7 correct probabilities linked with correct outcomes, may not be in table. Decimals correct to at least 3 SF. <b>SC B1</b> 7 or more probabilities summing to 1 placed in a probability distribution table.																
									<b>3</b>																	

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Question	Answer	Marks	Guidance
3(b)	$[E(X) =] [0] + 2 \times \frac{2}{12} + 4 \times \frac{2}{12} + 6 \times \frac{2}{12} + 8 \times \frac{1}{12} + 10 \times \frac{1}{12} + 12 \times \frac{1}{12}$ $\left[ [0] + \frac{4}{12} + \frac{8}{12} + \frac{12}{12} + \frac{8}{12} + \frac{10}{12} + \frac{12}{12} = \frac{54}{12} = 4.5 \right]$	<b>M1</b>	<p>Accept unsimplified expression. May be calculated in variance.</p> <p>Accept <math>\frac{1}{3} + \frac{2}{3} + 1 + \frac{2}{3} + \frac{5}{6} + 1</math> OE for the M mark FT <i>their</i> table with 7 or 8 probabilities summing to <math>0.999 \leq total \leq 1</math> (<math>0 &lt; p &lt; 1</math>).</p> <p>FT acceptable at the bold partially evaluated stage.</p>
	$[Var(X) =]$ $[0] + 2^2 \times \frac{2}{12} + 4^2 \times \frac{2}{12} + 6^2 \times \frac{2}{12} + 8^2 \times \frac{1}{12} + 10^2 \times \frac{1}{12} + 12^2 \times \frac{1}{12} - (their\ 4.5)^2$ $\left[ \frac{[0] + 2 \times 4 + 2 \times 16 + 2 \times 36 + [1 \times] 64 + [1 \times] 100 + [1 \times] 144}{12} - \frac{81}{4} \right]$ $[ = 35 - 4.5^2 ]$	<b>M1</b>	<p>Appropriate variance formula using <i>their</i> <math>(E(X))^2</math> value. FT <i>their</i> table with 6 or more probabilities. (<math>0 &lt; p &lt; 1</math>) which need not sum to 1 or with an expression no more evaluated than shown.</p> <p>FT acceptable at the bold partially evaluated stage with <i>their</i> probabilities.</p>
	$= 14.75, 14\frac{3}{4}$	<b>A1</b>	<p>CAO</p> <p>Accept <math>\frac{59}{4}</math>.</p> <p>If either or both M marks not awarded, <b>SC B1</b> for correct answer WWW</p>
		<b>3</b>	

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Question	Answer	Marks	Guidance
4(a)	$P(X < 18.2) = P\left(Z < \frac{18.2 - 19.8}{2.4}\right)$	<b>M1</b>	Use of $\pm$ standardisation formula with 18.2, 19.8 and 2.4 substituted appropriately, no continuity correction. Condone $\sigma^2(2.4^2)$ or $\sqrt{\sigma}(\sqrt{2.4})$ .
	$= [\Phi(-0.6667) = 1 - \Phi(0.6667)]$ $= 1 - 0.7477$	<b>M1</b>	Calculating the appropriate probability areas (leading to their final answer, expect $< 0.5$ ). Note: 0.432 is z-value of 0.667 so is not an appropriate probability area (M0).
	$= 0.252(3)$	<b>A1</b>	AWRT 0.252 SOI, accept 0.2525. If one or both M marks not awarded, <b>SC B1</b> for AWRT 0.252 SOI, accept 0.2525.
	[Expected number = $0.2523 \times 450 = 113.5$ ,] $= 113$ or $114$	<b>B1FT</b>	Strict FT <i>their</i> at least 4 figure probability $\times 450$ . (Check with calculator). One integer answer only. No indication of ‘approximation’, e.g. $\approx, \cong, about$ .
		<b>4</b>	
4(b)	$P(X > 25.5) = 0.26$ so $P\left(Z > \frac{25.5 - 23.4}{\sigma}\right) = 0.26$	<b>B1</b>	$0.643 \leq z \leq 0.6435$ or $-0.6435 \leq z \leq -0.643$ seen.
	$\frac{25.5 - 23.4}{\sigma} = 0.643$	<b>M1</b>	$\pm$ standardisation formula with 25.5, 23.4, $\sigma$ equating to a z-value, (not $1 - \text{their } z\text{-value} \dots$ ). Condone continuity correction $\pm 0.05$ , not $\sigma^2$ , not $\sqrt{\sigma}$ .
	$\sigma = 3.27$	<b>A1</b>	$3.26 \leq \sigma \leq 3.27$ . Do not award for improper fractions.
		<b>3</b>	

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Question	Answer				Marks	Guidance
5(a)	${}^{10}C_4 \times {}^6C_2 \times {}^5C_1$				<b>M1</b>	${}^{10}C_a \times {}^6C_b \times {}^5C_c$ , $a + b + c = 7$ , $a, b, c$ integers. No other terms present but condone $\times 6$ or $\times 3!$ .
	$[ = 210 \times 15 \times 5 ] = 15750$				<b>A1</b>	
					<b>2</b>	
5(b)	Scenario	V G P			<b>M1</b>	One product using 2 or 3 combinations with upper numbers correct and lower numbers summing to 5 and linked to a correct identified scenario. Condone the consistent use of permutations.
	VVVVG	4 1 0	${}^{10}C_4 \times {}^6C_1 [\times {}^5C_0]$	[1260 ]		
	VVVGG	3 2 0	${}^{10}C_3 \times {}^6C_2 [\times {}^5C_0]$	[1800 ]	<b>B1</b>	2 identified outcomes evaluated accurately, accept unsimplified.
	VVG GG	2 3 0	${}^{10}C_2 \times {}^6C_3 [\times {}^5C_0]$	[900]	<b>M1</b>	Add values of 5 correct scenarios, no incorrect/repeated scenarios.
	VVVGP	3 1 1	${}^{10}C_3 \times {}^6C_1 \times {}^5C_1$	[3600 ]		
	VVG GP	2 2 1	${}^{10}C_2 \times {}^6C_2 \times {}^5C_1$	[3375 ]		
	Total = 10935				<b>A1</b>	If either or both Ms not awarded, <b>SC B1</b> for 10935 WWW
					<b>4</b>	

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Question	Answer	Marks	Guidance																		
6(a)	<table><thead><tr><th>Falcons</th><th></th><th>Kites</th></tr></thead><tbody><tr><td>9 8</td><td>3</td><td>2</td></tr><tr><td>8 6 4 2</td><td>4</td><td>0 0 5 7 8</td></tr><tr><td>9 8 6 2 1 0</td><td>5</td><td>2 4 8 9 9</td></tr><tr><td>9 4</td><td>6</td><td>0 1 3 5</td></tr><tr><td>6</td><td>7</td><td></td></tr></tbody></table> <p>Key: 1 5 4 means 51 minutes for Falcons and 54 minutes for Kites</p>	Falcons		Kites	9 8	3	2	8 6 4 2	4	0 0 5 7 8	9 8 6 2 1 0	5	2 4 8 9 9	9 4	6	0 1 3 5	6	7		<b>B1</b>	Correct stem, ignore extra values (not in reverse, not split). If a split stem-and-leaf plot is used (i.e. stem values are repeated) the remaining B marks are available.
	Falcons		Kites																		
	9 8	3	2																		
	8 6 4 2	4	0 0 5 7 8																		
	9 8 6 2 1 0	5	2 4 8 9 9																		
9 4	6	0 1 3 5																			
6	7																				
<b>B1</b>	Correct Falcons labelled on left, leaves in order from right to left and lined up vertically, no commas or other punctuation.																				
<b>B1</b>	Correct Kites labelled on same diagram, leaves in order and lined up vertically, no commas or other punctuation.  Penalise each error only once in question. E.g. commas in both sets of data.																				
<b>B1</b>	Correct key, for their diagram, need both teams names and ‘mins’ at least once here, or in leaf headings or title.  <u>If 2 separate diagrams drawn</u> max marks <b>B1</b> if both stems correct. <b>B1</b> if Falcons correct to the left of the stem. <b>B1</b> if both keys correct including ‘mins’ and team name.																				
<b>4</b>																					
6(b)	Median = 51 [minutes]	<b>B1</b>	Accept <b>Q2</b> , <b>must</b> be identified.																		
	[IQR =] 59 – 44	<b>M1</b>	58 ≤ UQ ≤ 64 – 42 ≤ LQ ≤ 46. Implied if both quartile values are stated and an appropriate IQR calculated accurately.																		
	= 15 [minutes]	<b>A1</b>	WWW																		
		<b>3</b>																			

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Question	Answer	Marks	Guidance
6(c)	$\left[ \text{mean} = \frac{792 + 783}{30} = \frac{1575}{30} = \right] 52.5, 52\frac{1}{2}, \frac{105}{2}$	<b>B1</b>	$\frac{1575}{30}$ is not acceptable for this mark.
	$\Sigma'x^2 = 85727$ $\text{sd}^2 = [\text{Variance} =] \left[ \frac{(43504 + 42223)}{30} - \left( \frac{792 + 783}{30} \right)^2 \right]$ $\frac{85727}{30} - \left( \frac{1575}{30} \right)^2 [= 101.3167]$	<b>M1</b>	Accept unsimplified variance formula. FT <i>their</i> mean. Ignore any square root leading to sd for this mark.
	$\sigma = (\sqrt{101.3167}) = 10.1$	<b>A1</b>	AWRT. Must be identified, e.g. sd, s, std d, $\sigma$ . Condone ‘short’ square root signs. If M1 not awarded, <b>SC B1</b> for, $\sigma = \sqrt{101.3167}$ or $\sqrt{\frac{6079}{60}}$ oe = 10.1.
		<b>3</b>	

Question	Answer	Marks	Guidance
7(a)	$[(0.6)^4 \times 0.4 =] 0.0518[4], \frac{162}{3125}$	<b>B1</b>	
		<b>1</b>	

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Question	Answer	Marks	Guidance
7(b)	<b>Method 1</b>		
	$[P(X \leq 7) - P(X \leq 2) =] (1 - 0.6^7) - (1 - 0.6^2)$	<b>M1</b>	$(1 - p^7) - (1 - p^2)$ or $p^2 - p^7$ seen, $0 < p < 1$ .
	$[= 0.36 - 0.02799]$ $= 0.332[0 \dots], \frac{25938}{78125}$	<b>A1</b>	If M0 awarded <b>SC B1</b> 0.3320064 or $\frac{25938}{78125}$ CAO.
	<b>Method 2</b>		
	$[P(X = 3, 4, 5, 6, 7) =]$ $0.4 \times 0.6^2 + 0.4 \times 0.6^3 + 0.4 \times 0.6^4 + 0.4 \times 0.6^5 + 0.4 \times 0.6^6$	<b>M1</b>	$(1 - p) \times p^2 + (1 - p) \times p^3 + (1 - p) \times p^4 + (1 - p) \times p^5 + (1 - p) \times p^6$ seen, $0 < p < 1$ .
	$[= 0.144 + 0.0864 + 0.05184 + 0.031104 + 0.0186624]$ $= 0.332[0 \dots], \frac{25938}{78125}$	<b>A1</b>	If M0 awarded <b>SC B1</b> 0.3320064 or $\frac{25938}{78125}$ CAO.
	<b>Method 3 – geometric series</b>		
	$[P(X = 3, 4, 5, 6, 7) =] \frac{0.144(1 - 0.6^5)}{1 - 0.6 \text{ or } 0.4}$	<b>M1</b>	$\frac{0.144(1 - p^5)}{1 - p}$ seen $0 < p < 1$ .
	$= 0.332[0 \dots], \frac{25938}{78125}$	<b>A1</b>	If M0 awarded <b>SC B1</b> 0.3320064 or $\frac{25938}{78125}$ CAO.
		<b>2</b>	



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Question	Answer	Marks	Guidance
7(c)	<b>Method 1</b>		
	2nd goal scored on:		
	2nd attempt	$(0.4)^2$	[ = 0.16]
	3rd attempt	$(0.4)^2 (0.6) \times (2 \text{ or } {}^2C_1)$	[ = 0.192]
	4th attempt	$(0.4)^2 (0.6)^2 \times (3 \text{ or } {}^3C_1)$	[ = 0.1728]
	5th attempt	$(0.4)^2 (0.6)^3 \times (4 \text{ or } {}^4C_1)$	[ = 0.13824]
	$= 0.663, \frac{2072}{3125}$	<b>A1</b>	If either or both M marks not awarded, <b>SC B1</b> for 0.663, $\frac{2072}{3125}$ WWW condone 1 index error.
	<b>Method 2</b>		
	${}^5C_2(0.4)^2(0.6)^3 + {}^5C_3(0.4)^3(0.6)^2 + {}^5C_4(0.4)^4(0.6)^1 + {}^5C_5(0.4)^5$ [0.3456 + 0.2304 + 0.0768 + 0.01024] or $1 - ({}^5C_0 (0.6)^5 + {}^5C_1(0.4)^1(0.6)^4)$	<b>M1</b>	At least 2 correct unsimplified terms.
		<b>M1</b>	Add values for 4 terms of the form ${}^5C_a(0.4)^a(0.6)^{5-a}$ or $1 - \text{sum of 2 terms of the form } {}^5C_a(0.4)^a(0.6)^{5-a}.$
	$= 0.663, \frac{2072}{3125}$	<b>A1</b>	If either or both M marks not awarded, <b>SC B1</b> for 0.663 www condone 1 index error.
		<b>3</b>	

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Question	Answer	Marks	Guidance
7(d)	[Mean = $75 \times 0.4 =$ ] 30 [Variance = $75 \times 0.4 \times 0.6 =$ ] 18	<b>B1</b>	30 and 18 seen, allow unsimplified. May be seen in standardisation formula. ( $\sigma = \sqrt{18}, 3\sqrt{2}, 4.2426 \leq \sigma \leq 4.243$ implies correct variance) Withhold mark if variance clearly identified as standard deviation.
	$P(28 < X < 35) = P\left(\frac{28.5 - 30}{\sqrt{18}} < Z < \frac{34.5 - 30}{\sqrt{18}}\right)$	<b>M1</b>	Substituting <i>their</i> $\mu$ and positive $\sigma$ into one $\pm$ standardising formula (any number for 28.5 or 34.5), not $\sigma^2$ , not $\sqrt{\sigma}$ .
		<b>M1</b>	Using continuity corrections 27.5 <i>or</i> 28.5 and 34.5 <i>or</i> 35.5 in <i>their</i> 2 separate standardisation formula.
	$[= \Phi(1.0607) + \Phi(0.3536) - 1]$ = 0.8556 + 0.6383 – 1 Or 0.8556 – (1 – 0.6383) Or 0.8556 – 0.3617 Or (0.8556 – 0.5) + (0.6383 – 0.5) Or 0.3556 + 0.1383	<b>M1</b>	Appropriate area $\Phi$ , from final process. Must be a probability.
	= 0.494	<b>A1</b>	AWRT.
		<b>5</b>	